

Suite géométrique

$$U_{n+1} = U_n \times q$$

$$\frac{U_{n+1}}{U_n} = q$$

si $q > 1$ (U_n) croissante

si $0 < q < 1$ (U_n) décroissante

Sens de variation de (w_n)

$$w_n = \frac{2^n}{5^n}$$

$$1 \rightarrow w_{n+1} = \frac{2^{n+1}}{5^{n+1}}$$

$$\rightarrow a^m \times a^n = a^{m+n}$$

$$2 \rightarrow \frac{w_{n+1}}{w_n} = \frac{\frac{2^{n+1}}{5^{n+1}}}{\frac{2^n}{5^n}} = \frac{2^{n+1}}{5^{n+1}} \times \frac{5^n}{2^n} = \frac{\cancel{2^n} \times 2}{\cancel{5^n} \times 5} \times \frac{\cancel{5^n}}{\cancel{2^n}} = \frac{2}{5}$$

Rappel:

$$\frac{a/b}{c/d} = \frac{a}{b} \times \frac{d}{c}$$

$$\frac{w_{n+1}}{w_n} = \frac{2}{5} \quad 0 < \frac{2}{5} < 1 \quad 3$$

donc (w_n) décroissante

Sens de variation

$$U_n = 3^n \quad \rightarrow \quad U_{n+1} = 3^{n+1}$$

$$\frac{U_{n+1}}{U_n} = \frac{3^{n+1}}{3^n} = \frac{3^n \times 3}{3^n} = 3$$

$$\frac{U_{n+1}}{U_n} = 3 \quad 3 > 1 \quad \leftarrow 3$$

donc (U_n) est croissante

Sens de variation

$$U_n = \frac{2^{n+3}}{3^n}$$

$$U_{n+1} = \frac{2^{(n+1)+3}}{3^{n+1}} = \frac{2^{n+4}}{3^{n+1}}$$

$$\begin{aligned} \frac{U_{n+1}}{U_n} &= \frac{\frac{2^{n+4}}{3^{n+1}}}{\frac{2^{n+3}}{3^n}} = \frac{2^{n+4}}{3^{n+1}} \times \frac{3^n}{2^{n+3}} = \frac{\cancel{2^n} \times 2^4}{\cancel{3^n} \times 3} \times \frac{\cancel{3^n}}{\cancel{2^n} \times 2^3} \\ &= \frac{2^4}{3 \times 2^3} = \frac{2}{3} \quad 0 < \frac{2}{3} < 1 \end{aligned}$$

donc (U_n) est décroissante

Suite arithmétique

$$U_0 = -1 \quad r = 2 \quad U_{30} = ?$$

$$U_n = U_0 + nr$$

$$U_{30} = -1 + 30 \times 2$$

$$U_{30} = 59$$

Calculer

$$S = -4 - 1 + 2 + 5 + \dots + 35$$

9
premier

↑
dernier